MARK SCHEME for the May/June 2010 question paper

for the guidance of teachers

9709 MATHEMATICS

9709/23

Paper 23, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

- AEF Any Equivalent Form (of answer is equally acceptable)
- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- CWO Correct Working Only often written by a 'fortuitous' answer
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)
- SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR -1 A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through $\sqrt{"}$ marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA -1 This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.

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1		nply $y \log 2.8 = x \log 13$		B1	
	Rearrange	e into form $y = \frac{\log 13}{\log 2.8}x$ or equivalent		B1	
	Obtain an	swer $k = 2.49$		B1	[3]
2		State or imply correct ordinates 0.27067, 0.20521, 0.1493 Use correct formula, or equivalent, correctly with $h = 0.5$ and Obtain answer 0.21 with no errors seen		B1 M1 A1	[3]
	(ii)	Justify statement that the trapezium rule gives an over-estimate	te	B1	[1]
3	EITHER OR	State or imply non-modular inequality $(2x-1)^2 < (x+4)^2$, or or pair of linear equations Make reasonable solution attempt at a 3-term quadratic, or s Obtain critical values -1 and 5 State correct answer $-1 < x < 5$ Obtain one critical value, e.g. $x = 5$, by solving a linear equa from a graphical method or by inspection Obtain the other critical value similarly State correct answer $-1 < x < 5$	olve two linear equations	M1 A1 A1 B1 B2 B1	[4]
4		in integral $a \sin 2x$ with $a = \pm \left(1, 2 \text{ or } \frac{1}{2}\right)$ limits and obtain $\frac{1}{2}$ (AG)		M1 A1	[2]
	Obta Atter	$tan^2 x = \sec^2 x - 1$ and attempt to integrate both terms in $3tan x - 3x$ mpt to substitute limits, using exact values in answer $2\sqrt{3} - \frac{\pi}{2}$		M1 A1 M1 A1	[4]
5		Use product rule Obtain correct derivative in any form Show that derivative is equal to zero when $x = 3$		M1 A1 A1	[3]
		Substitute $x = 1$ into gradient function, obtaining $2e^{-1}$ or equiv State or imply required <i>y</i> -coordinate is e^{-1} Form equation of line through (1, e^{-1}) with gradient found (NO Obtain equation in any correct form		M1 B1 M1 A1	[4]
6		Make a recognisable sketch of a relevant graph, e.g. $y = \ln x$ c Sketch a second relevant graph and justify the given statemen		B1 B1	[2]
		Consider sign of In $x - (2 - x^2)$ at $x = 1.3$ and $x = 1.4$, or equiv Complete the argument correctly with appropriate calculation		M1 A1	[2]

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(iii)	Show that given equation is equivalent to $x = \sqrt{(2 - \ln x)}$	\overline{x}) or vice versa	B1	[1
(iv)	Use the iterative formula correctly at least once Obtain final answer 1.31		M1 A1	
	Show sufficient iterations to justify its accuracy to 2 d.p in the interval (1.305, 1.315)	o. or show there is a sign ch	ange B1	[3
(i)	Substitute $x = 3$ and equate to 30		M1	
	Substitute $x = -1$ and equate to 18 Obtain a correct equation in any form Solve a relevant pair of equations for <i>a</i> or for <i>b</i>		M1 A1 M1	
	Obtain $a = 1$ and $b = -13$		A1	[5
(ii)	Either show that $f(2) = 0$ or divide by $(x - 2)$, obtaining Obtain quadratic factor $2x^2 + 5x - 3$	a remainder of zero	B1 B1	
	Obtain linear factor $2x - 1$ Obtain linear factor $x + 3$ [Condone omission of repetition that $x - 2$ is a factor.]		B1 B1	
	[If linear factors $2x - 1$, $x + 3$ obtained by remainder the	eorem or inspection, award	B2 + B1.]	[4
(i)	Use correct $sin(A - B)$ and $cos(A - B)$ formulae Substitute exact values for sin 30° etc.		M1 M1	
	Obtain given answer correctly		A1	[3
(ii)	State $\sqrt{3}\sin x = \frac{1}{2}\sec x$		B1	
	Rearrange to $\sin 2x = k$, where k is a non-zero constant		M1	
	Carry out evaluation of $\frac{1}{2}\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$		M1	
	Obtain answer 17.6°		A1	
	Carry out correct method for second answer Obtain remaining 3 answers from 17.6°, 72.4°, 197.6°,	252.4° and no others in the	M1	
	range		A1	[6