Cambridge International AS & A Level

MATHEMATICS **9709/04**

Paper 4 Mechanics **For examination from 2020**

MARK SCHEME

Maximum Mark: 50

Specimen

This document has **10** pages. Blank pages are indicated.

SPECIMEN

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:
Marks must be awarded in line with:
• the specific content of the mark scheme or the generic level descriptors for the question   • the specific skills defined in the mark scheme or in the generic level descriptors for the question   • the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:
Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:
Marks must be awarded **positively**:
• marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate   • marks are awarded when candidates clearly demonstrate what they know and can do   • marks are not deducted for errors   • marks are not deducted for omissions   • answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:
Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mark Scheme Notes

Marks are of the following three types.

M	Method mark, given for a valid method applied to the problem. Method marks can still be given even if there are numerical errors, algebraic slips or errors in units. However the method must be applied to the specific problem, e.g. by substituting the relevant quantities into a formula. Correct use of a formula without the formula being quoted earns the M mark and in some cases an M mark can be implied from a correct answer.
A	Accuracy mark, given for an accurate answer or accurate intermediate step following a correct method. Accuracy marks cannot be given unless the relevant method mark has also been given.
B	Mark for a correct statement or step.
DM or DB	M marks and B marks are generally independent of each other. The notation DM or DB means a particular M or B mark is dependent on an earlier M or B mark (indicated by *). When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT below).
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures (sf) or would be correct to 3 sf if rounded (1 decimal point (dp) for angles in degrees). As stated above, an A or B mark is not given if a correct numerical answer is obtained from incorrect working.
- Common alternative solutions are shown in the Answer column as: '**EITHER** Solution 1 **OR** Solution 2 **OR** Solution 3 …'. Round brackets appear in the Partial Marks column around the marks for each alternative solution.
- Square brackets [ ] around text show extra information not needed for the mark to be awarded.
- The total number of marks available for each question is shown at the bottom of the Marks column in bold type.
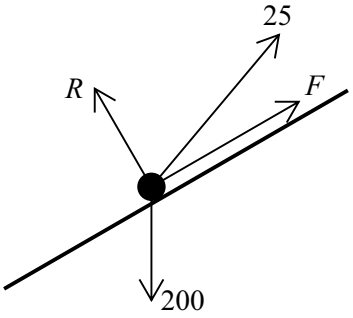
The following abbreviations may be used in a mark scheme.

AG	Answer given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid).
CAO	Correct answer only (emphasising that no 'follow through' from an error is allowed).
CWO	Correct working only
FT	Follow through after error (see Mark Scheme Notes for further details).
ISW	Ignore subsequent working
OE	Or equivalent form
SC	Special case
SOI	Seen or implied

Question	Answer	Marks	Partial Marks	Guidance
1(a)	$0 = 20^2 - 20s$	1	**M1**	For using $v^2 = u^2 + 2as$ with $a = -10$ to find s, the greatest height reached
	$s = 20\,\text{m}$	1	**A1**	
		2		
1(b)	$0 = 20 - 10t$ $t = 2$	1	**M1**	For using $v = u + at$ with $v = 0$, $u = 20$ and $a = -10$ to find the time to the greatest height
	Total time $4\,\text{s}$	1	**A1**	
		2		

Question	Answer	Marks	Partial Marks	Guidance
2(a)	$[DF = 1350]$ Power $= 1350 \times 32$	1	**M1**	
	$= 43.2\,\text{kW}$	1	**A1**	
		2		
2(b)	$DF - 1350 + 1200g \times \frac{1}{20} = 0$ $[DF = 750]$	1	**M1**	For using Newton's 2nd law applied to the car down the hill (3 terms) Allow use of $\theta = 2.9°$
	$31\,500 = $ their $(750) \times v$	1	**M1**	For using $DF = \dfrac{P}{v}$
	$v = 42\,\text{m s}^{-1}$	1	**A1**	
		3		

Question	Answer	Marks	Partial Marks	Guidance
3(a)	Conservation of momentum $4 \times 6 \ [+ 0] = 4 \times 2 + 2v$	1	**M1**	For applying conservation of momentum
	$v = 8 \ [\mathrm{m\,s^{-1}}]$	1	**A1**	
		2		
3(b)	$2 \times$ their (8) $[+ 0] = 2v + 3v$	1	**M1**	For applying conservation of momentum
	$v = 3.2 \ [\mathrm{m\,s^{-1}}]$	1	**A1**	
		2		
3(c)	Kinetic energy (KE) initial $= \frac{1}{2} \times 4 \times 6^2$ KE final $= \frac{1}{2} \times 4 \times 2^2 + \frac{1}{2} \times 5 \times 3.2^2$	1	**M1**	For use of $\frac{1}{2} \times m \times v^2$, when either initial or final calculation correct using their value from **(b)**
	Loss of KE $= 72 - 33.6 = 38.4 \ [\mathrm{J}]$	1	**A1**	AG For all correct
		2		

Question	Answer	Marks	Partial Marks	Guidance
4(a)	Correct force diagram with 3 extra forces shown 	1	B1	Accept 200 or 20 g for weight
4(b)	For resolving forces in the direction parallel to and/or perpendicular to the plane	1	M1	
	$F + 25\cos 20° = 20 \times g \times \sin 30°$	1	A1	
	$R + 25\sin 20° = 20 \times g \times \cos 30°$	1	A1	
	$[F = 76.5...]$ $[R = 164.65...]$ $\mu = \dfrac{\text{their }(76.5...)}{\text{their }(164.65...)}$	1	M1	Use $F = \mu R$ to evaluate μ
	$= 0.465$	1	A1	
		5		

Question	Answer	Marks	Partial Marks	Guidance
5(a)	$2500 - 2000g \times 0.1 - 400 = 2000a$	1	**M1**	For Newton's 2nd law
	$a = 0.05\,\mathrm{m\,s}^{-2}$	1	**A1**	
	$2500 - T - 300 - 1200g \times 0.1 = 1200 \times 0.05$ **OR** $T - 100 - 800g \times 0.1 = 800 \times 0.05$	1	**M1**	For Newton's 2nd law to either car or trailer to give an equation for T.
	$T = 940\,\mathrm{N}$	1	**A1**	
		4		
5(b)	$-2000g \times 0.1 - 400 = 2000a$ $[a = -1.2]$	1	**M1**	For Newton's 2nd law
	$0 = 30 - 1.2t$	1	**M1**	For using $v = u + at$
	$t = 25\,\mathrm{s}$	1	**A1**	
	$T - 100 - 800g \times 0.1 = 800 \times -1.2$	1	**M1**	For applying Newton's second law to the trailer or to the car
	$T = -60\,\mathrm{N}$	1	**A1**	Accept (thrust) = 60N
		5		

Question	Answer	Marks	Partial Marks	Guidance
6(a)	$k = 40$	**1**	**B1**	
6(b)	$$\begin{bmatrix} y = 5x^2 - 10x & \text{for } 0 \leqslant x \leqslant 4, \\ y = 40 & \text{for } 4 \leqslant x \leqslant 14, \\ y = 68 - 2x & \text{for } 14 \leqslant x \leqslant 20 \end{bmatrix}$$	1	**B1FT**	Correct for $0 \leqslant t \leqslant 4$ For quad graph, min at $t = 1$; FT on k
		1	**B1FT**	Correct for $4 \leqslant t \leqslant 14$ For horizontal line at $v = k$; FT on k
		1	**B1FT**	Correct for $14 \leqslant t \leqslant 20$ For line with negative gradient from $(14, k)$ to $(20, 28)$ [gradient $= -2$]; FT on k
		3		
6(c)	$a = 10t - 10$	1	**M1**	For attempting to differentiate to find a
	$1 < t < 4$	1	**A1**	Allow $\leqslant$ at 4 but not at 1
		2		
6(d)	Dist = $\left\| \int_0^2 (5t^2 - 10t)\,dt \right\| + \int_2^4 (5t^2 - 10t)\,dt + (40 \times 10) + (0.5 \times (40 + 28) \times 6)$	1	**M1**	For attempting to integrate
		1	**A1**	For correct expression including limits and the distance travelled over full 20 s
		1	**B1**	For correct integration
	$= \left\| \left[\frac{5}{3}t^3 - 5t^2 \right]_0^2 \right\| + \left[\frac{5}{3}t^3 - 5t^2 \right]_2^4 + 400 + 204$	1	**A1FT**	FT on their k
	$= 644\,\text{m}$	1	**A1**	
		5		

Question	Answer	Marks	Partial Marks	Guidance
7(a)	**EITHER** Solution 1 $T = 0.8a$ for A $0.2g - T = 0.2a$ for B $0.2g = (0.2 + 0.8)a$ for system	2	(M1M1	M1 for applying Newton's 2nd law either to particle A or to particle B or to the system M1 for applying Newton's 2nd law to a second particle (if needed) and solving for a
	$a = 2$	1	A1	
	$2.5 = 0.5 \times 2 \times t^2$	1	M1	For using a complete method for finding t such as using $s = ut + \frac{1}{2}at^2$
	$t = 1.58\,\text{s}$	1	A1)	Allow $t = \frac{1}{2}\sqrt{10}$
	OR Solution 2 $0.2 \times g \times 2.5$ **OR** $\frac{1}{2}(0.2 + 0.8)v^2$	1	(M1	For finding potential energy (PE) loss or KE gain (system)
	$0.2 \times g \times 2.5 = \frac{1}{2}(0.2 + 0.8)v^2$	1	M1	For using PE loss = KE gain and finding v
	$v^2 = 10$	1	A1	
	$2.5 = \frac{1}{2}(0 + \sqrt{10})t$	1	M1	For using $s = \frac{1}{2}(u + v)t$
	$t = 1.58\,\text{s}$	1	A1)	Allow $t = \frac{1}{2}\sqrt{10}$
	OR Solution 3 $T = 0.8a$ $0.2g - T = 0.2a$ $\rightarrow T = 1.6\,\text{N}$	1	(M1	For applying Newton's 2nd law to A and B and solving for T
	$T \times 2.5 = \frac{1}{2}(0.8)v^2$	1	M1	For using work done (WD) by T = KE gain by A, find v
	$v^2 = 10$	1	A1	
	$2.5 = \frac{1}{2}(0 + \sqrt{10})t$	1	M1	For using $s = \frac{1}{2}(u + v)t$
	$t = 1.58\,\text{s}$	1	A1)	Allow $t = \frac{1}{2}\sqrt{10}$
	Available marks	5		

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Question	Answer	Marks	Partial Marks	Guidance
7(b)	$0.2 \times g \times 2.5 = \frac{1}{2}(0.8 + 0.2)v^2 + 2$	2	**M1A1**	M1 For applying work/energy to the system as PE loss = KE gain + WD against resistance A1 For correct work/energy equation
	For solving for v	1	**M1**	
	$v = \sqrt{6}$ (or 2.45)	1	**A1**	
		4		