READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use a soft pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.
If working is needed for any question it must be shown below that question.
Electronic calculators should be used.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For π, use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total of the marks for this paper is 104.
Aida, Bernado and Cristiano need $30 000 to start a business.

(a) (i) They borrow \( \frac{2}{5} \) of this amount.

Show that they still need $18 000.

Answer (a)(i)

(ii) They provide the $18 000 themselves in the ratio

Aida : Bernado : Cristiano = 5 : 4 : 3.

Calculate the amount each of them provides.

Answer (a)(ii)

B

(i) Office equipment costs 35% of the $30 000.

Calculate the cost of the equipment.

Answer (b)(i)

(ii) Office expenses cost another $6500.

Write this as a fraction of $30 000.

Give your answer in its lowest terms.

Answer (b)(ii)

(iii) How much remains of the $30 000 now?

Answer (b)(iii)

(c) They invest $12 500.

After one year this has increased to $15 500.

Calculate this percentage increase.

Answer (c)
ABCD represents a building with a vertical flagpole, AF, on the roof. The points E, D and C are on level ground. EA = 55 metres. The angle of elevation of A from E is 18° and the angle of elevation of F from E is 25°.

(a) Calculate
   (i) ED,

   Answer(a)(i) ........................................ m [2]

   (ii) FD,

   Answer(a)(ii) ........................................ m [2]

   (iii) DA.

   Answer(a)(iii) ........................................ m [2]

(b) Show that AF = 7.4 metres, correct to 1 decimal place.  
   Answer(b) [1]

(c) The width, AB, of the building is 12 metres. The top of the flagpole is attached to the point B by a rope. Calculate
   (i) the length of the rope, FB,

   Answer(c)(i) ........................................... m [2]

   (ii) the angle of elevation of F from B.

   Answer(c)(ii) ........................................... [2]
The table below shows the average daily sunshine, \( s \), and the total monthly rainfall, \( r \), for a city during one year.

<table>
<thead>
<tr>
<th>Month</th>
<th>Jan</th>
<th>Feb</th>
<th>Mar</th>
<th>Apr</th>
<th>May</th>
<th>June</th>
<th>July</th>
<th>Aug</th>
<th>Sep</th>
<th>Oct</th>
<th>Nov</th>
<th>Dec</th>
</tr>
</thead>
<tbody>
<tr>
<td>( s ) (hours)</td>
<td>6</td>
<td>7</td>
<td>7</td>
<td>9</td>
<td>10</td>
<td>12</td>
<td>12</td>
<td>12</td>
<td>9</td>
<td>8</td>
<td>6</td>
<td>5</td>
</tr>
<tr>
<td>( r ) (mm)</td>
<td>70</td>
<td>52</td>
<td>72</td>
<td>41</td>
<td>20</td>
<td>6</td>
<td>1</td>
<td>4</td>
<td>16</td>
<td>52</td>
<td>65</td>
<td>67</td>
</tr>
</tbody>
</table>

(a) For \( s \), find

(i) the mode

Answer(a)(i) ........................................ hours [1]

(ii) the range,

Answer(a)(ii) ........................................ hours [1]

(iii) the median.

Answer(a)(iii) ........................................ hours [2]

(b) On the grid below, plot the 10 points for March to December to complete the scatter diagram.
(c) (i) Calculate the mean of $s$.

Answer (c)(i) ........................................ hours [2]

(ii) The mean of $r$ is 38.8 millimetres.
On the grid, plot the point representing these means. Label this point M. [1]

(d) (i) Draw a line of best fit on the grid. [1]

(ii) What type of correlation does your scatter diagram show?

Answer (d)(ii) ........................................... [1]

4

$EG$ is a diameter of the circle through $E, C$ and $G$.
The tangent $AEB$ is parallel to $CD$ and angle $AEC = 68^\circ$.
Calculate the size of the following angles and give a reason for each answer.

(a) Angle $CEG = ........................................$ because .......................................................... [2]

(b) Angle $ECG = ........................................$ because .......................................................... [2]

(c) Angle $CGE = ........................................$ because .......................................................... [2]

(d) Angle $ECD = ........................................$ because .......................................................... [2]
Aminata and her brother live 18 kilometres from a shopping centre.

(a) Aminata leaves home at 09:00 and runs 3 kilometres to a bus stop. She arrives there at 09:30.

Write down her average speed, in kilometres per hour.

Answer (a) \( \frac{3}{0.5} \) km/h [1]

(b) She waits 15 minutes for the bus.

The bus travels the remaining 15 kilometres to the shopping centre at an average speed of 20 km/h.

(i) At what time does she arrive at the shopping centre?

Answer (b)(i) \( 09:30 + \frac{15}{60} \) [2]

(ii) On the grid below, complete the travel graph showing her journey to the shopping centre.
(c) Her brother leaves home at 11:15. He travels to the shopping centre by car at an average speed of 54 km/h.

(i) Work out how long, in minutes, he takes to travel to the shopping centre.

\[ \text{Answer (c)(i)} \quad \text{.................................................. minutes} \quad [1] \]

(ii) Show his journey on the grid. \[ [1] \]

(d) Aminata and her brother leave the shopping centre at 12:00. They travel home by car and arrive at 12:45.

(i) Show their journey home on the grid. \[ [1] \]

(ii) Calculate the average speed of their journey home.

\[ \text{Answer (d)(ii)} \quad \text{.................................................. km/h} \quad [2] \]

6 (a) \[ 2y = 75 - 7x \]

(i) Find \( y \) when \( x = 7 \).

\[ \text{Answer (a)(i)} \quad y = \text{..................................................} \quad [2] \]

(ii) Find \( x \) when \( y = 6 \).

\[ \text{Answer (a)(ii)} \quad x = \text{..................................................} \quad [2] \]

(b) Make \( x \) the subject of the equation \( 2y = 75 - 7x \).

\[ \text{Answer (b)} \quad x = \text{..................................................} \quad [2] \]

(c) Solve these simultaneous equations.

\[
\begin{align*}
4x - y &= 45 \\
7x + 2y &= 75
\end{align*}
\]

\[ \text{Answer (c)} \quad x = \text{..................................................} \quad [3] \]

\[ y = \text{..................................................} \]
7 (a) Complete the table of values for the equation \( y = x^2 + x - 3 \).

<table>
<thead>
<tr>
<th>x</th>
<th>-4</th>
<th>-3</th>
<th>-2</th>
<th>-1</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
</tr>
</thead>
<tbody>
<tr>
<td>y</td>
<td>9</td>
<td>-1</td>
<td>-3</td>
<td>-1</td>
<td>9</td>
<td>-1</td>
<td>9</td>
<td></td>
</tr>
</tbody>
</table>

(b) On the grid, draw the graph of \( y = x^2 + x - 3 \).

(c) Write down the coordinates of the lowest point of the curve.

\[ Answer(c) \quad ( \quad , \quad ) \] [2]

(d) (i) Draw the line of symmetry of the graph.

(ii) Write down the equation of the line of symmetry.

\[ Answer(d)(ii) \quad \] [1]
Triangle $ABC$ is drawn on the grid.

(a) (i) Write down the coordinates of $A$.

Answer (a)(i) $(\ldots, \ldots)$ [1]

(ii) Write $\overrightarrow{AB}$ and $\overrightarrow{BC}$ as column vectors.

Answer (a)(ii) $\overrightarrow{AB} = \begin{pmatrix} \ldots \end{pmatrix}$ $\overrightarrow{BC} = \begin{pmatrix} \ldots \end{pmatrix}$ [2]

(b) Translate triangle $ABC$ by the vector $\begin{pmatrix} 4 \\ -3 \end{pmatrix}$. Label the image $T$. [2]

(c) $\overrightarrow{AP} = 2\overrightarrow{AB}$ and $\overrightarrow{AQ} = 2\overrightarrow{AC}$.

(i) Plot the points $P$ and $Q$ on the grid. [2]

(ii) Describe fully the single transformation which maps triangle $ABC$ onto triangle $APQ$.

Answer (c)(ii) 

[3]

(d) Rotate triangle $ABC$ through $180^\circ$ about the midpoint of the side $AB$. Label the image $R$. [2]
9 The quadrilateral $ABCD$ is a scale drawing of a park. Angle $ABC = 90^\circ$ and 1 centimetre represents 10 metres.

(a) Write down

(i) the actual length, in metres, of the side $CD$.

$Answer(a)(i)$ ........................................ m [1]

(ii) the size of angle $BAD$.

$Answer(a)(ii)$ ........................................ [1]

(b) Two straight paths cross the park.

One path is the same distance from $AB$ as from $BC$.
The other path is the same distance from $A$ as from $D$.

(i) Using a straight edge and compasses only, construct the lines which show each path. [4]

(ii) Tennis courts in the park are situated in a region closer to $AB$ than to $BC$ and closer to $A$ than to $D$. Label this region $T$. [1]

(c) Keith cycles past the park, so that he is always 30 metres outside the boundary $ABC$.

Construct the locus of points which shows this part of his route. [2]
The first three diagrams in a sequence are shown below. Each diagram has one more trapezium added on the right.

Diagram 1  
Diagram 2  
Diagram 3

(a) Complete the table which shows the number of lines and dots in each diagram.

<table>
<thead>
<tr>
<th>Diagram</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of lines</td>
<td>4</td>
<td>7</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Number of dots</td>
<td>4</td>
<td>6</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

(b) Find the number of lines and dots in Diagram 10.

Answer(b) ............ lines and ............ dots [2]

(c) For Diagram n, write down in terms of n, the number of

(i) lines,

Answer(c)(i) .................................. [2]

(ii) dots.

Answer(c)(ii) .................................. [2]

(d) Find the difference, in terms of n, between your answers to parts (c)(i) and (c)(ii).
Simplify your answer.

Answer(d) .................................. [2]