

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS Cambridge International Level 3 Pre-U Certificate Principal Subject

### MATHEMATICS

Additional Materials:

Paper 3 Applications of Mathematics

9794/03 October/November 2013 2 hours

Answer Booklet/Paper Graph Paper List of Formulae (MF20)

## READ THESE INSTRUCTIONS FIRST

If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet.

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a soft pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

Where a numerical value for the acceleration due to gravity is needed, use  $10 \text{ m s}^{-2}$ .

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 80.

You are advised to spend no more than 1 hour on Section A and 1 hour on Section B.

This document consists of 4 printed pages.



# Section A: Probability (40 marks)

### You are advised to spend no more than 1 hour on this section.

1 (i) Given that  $X \sim \text{Geo}\left(\frac{1}{6}\right)$ , write down the values of E(X) and Var(X). [2]

(ii) 
$$Y \sim B(n, p)$$
. Given that  $E(Y) = 4$  and  $Var(Y) = \frac{8}{3}$ , find the values of *n* and *p*. [3]

2 The random variable *X* is defined as the difference (always positive or zero) between the scores when 2 ordinary dice are rolled.

x	0	1	2	3	4	5
$\mathbf{P}(X=x)$						

(ii) Find the expectation and variance of *X*.

- 3 In a large examination room each candidate has just one electronic calculator.
  - G is the event that a randomly chosen candidate has a graphical calculator.
  - *T* is the event that a randomly chosen candidate has a 'Texio' brand calculator.

You are given the following probabilities.

$$P(G) = 0.65$$
  $P(T) = 0.4$   $P(G \cap T) = 0.25$ 

- (i) Are the events G and T independent? Justify your answer with an appropriate calculation. [2]
- (ii) Find  $P(T \mid G)$  and explain, in the context of this question, what this probability represents. [3]
- 4 As part of a study into the effects of alcohol, volunteers have their reaction times measured after they have consumed various fixed amounts of alcohol. For a random sample of 12 volunteers the following information was collected.

Units of alcohol consumed	2	3	3	4	4.5	5.5	6	6	7	8	8	9
Reaction time (seconds)	1	2	5	5	3.8	5.5	4.8	8.5	7.2	6.8	9	8

- (i) Which is the independent variable in this experiment?
- (ii) Find the least squares regression line of *y* (Reaction time) on *x* (Units of alcohol), and use it to estimate the reaction time of someone who has consumed 5 units of alcohol. [5]

[5]

[1]

5 The table summarises 43 birth weights as recorded for babies born in a particular hospital during one week.

Birth weight ( <i>w</i> kg)	$2.0 \leq w < 2.5$	$2.5 \leq w < 3.0$	$3.0 \leq w < 3.5$	$3.5 \leq w < 4.0$	$4.0 \leq w < 4.5$
Frequency	1	6	9	17	10

- (i) State the type of skewness of the data.
- (ii) Given that the lower quartile is 3.21 kg and the upper quartile is 3.96 kg, determine whether there are any babies whose birth weights might be regarded as outliers. [4]
- (iii) The mean birth weight was found to be 3.58 kg. However, it was discovered subsequently that the table includes the birth weight, 2.52 kg, of one baby that has been recorded twice. Find the mean birth weight after this error has been removed.
- 6 A company supplies tubs of coleslaw to a large supermarket chain. According to the labels on the tubs, each tub contains 300 grams of coleslaw. In practice the weights of coleslaw in the tubs are normally distributed with mean 305 grams and standard deviation 6 grams.
  - (i) Find the proportion of tubs that are underweight, according to the label. [3]

The supermarket chain requires that the proportion of underweight tubs should be reduced to 5%.

- (ii) If the standard deviation is kept at 6 grams, find the new mean weight needed to achieve the required reduction. [3]
- (iii) If the mean weight is kept at 305 grams, find the new standard deviation needed to achieve the required reduction. Explain why the company might prefer to adjust the standard deviation rather than the mean. [3]

#### Section B: Mechanics (40 marks)

#### You are advised to spend no more than 1 hour on this section.

- 7 10 seconds after passing a warning signal, a train is travelling at  $18 \text{ m s}^{-1}$  and has gone 215 m beyond the signal. Find the acceleration (assumed to be constant) of the train during the 10 seconds and its velocity as it passed the signal. [6]
- 8 A ball of mass 0.04 kg is released from rest at a height of 1 metre above a table. It rebounds to a height of 0.81 metre.
  - (i) Find the value of *e*, the coefficient of restitution. [4]
  - (ii) Find the impulse on the ball when it hits the table. [3]
- 9 A tennis ball is served horizontally at a speed of  $24 \text{ m s}^{-1}$  from a height of 2.45 m above the ground.
  - (i) Show that it will clear the net at a point where the net is 1 m high and 12 m from the server. [5]
  - (ii) How far beyond the net will it land?

[4]

[1]

12



(i) Find the tension in string *AP*.

[4]

- (ii) Explain why the parcel can never be in equilibrium with both strings horizontal. [1]
- 11 Two particles, A and B, each of mass 1 kg are connected by a light inextensible string. Particle A is at rest on a slope inclined at  $30^{\circ}$  to the horizontal. The string passes over a small smooth pulley at the top of the slope and particle B hangs freely, as shown in the diagram.



- (i) (a) In the case when the slope is smooth, draw a fully labelled diagram to show the forces acting on the particles. Hence find the acceleration of the particles and the tension in the string.
  - (b) Write down the direction of the resultant force exerted by the string on the pulley. [1]
- (ii) In fact the contact between particle A and the slope is rough. The coefficient of friction between A and the slope is  $\mu$ . The system is in equilibrium. Find the set of possible values of  $\mu$ . [5]

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

University of Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.